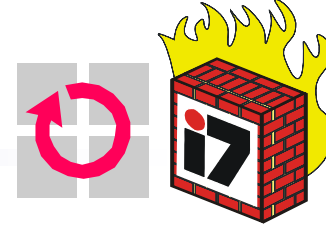


# Chapter 2

## Basics of Cryptography

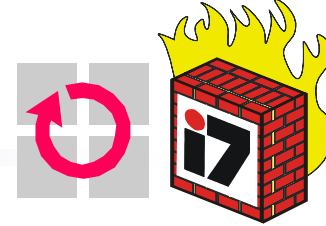
- ❑ Overview Cryptographic Algorithms
- ❑ Attacking Cryptography
- ❑ Properties of Encryption Algorithms
- ❑ Classification of Encryption Algorithms

# Cryptographic Algorithms: Overview



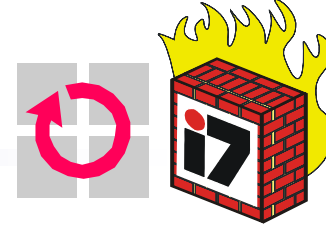
- ❑ During this course two main applications of cryptographic algorithms are of principal interest:
  - ❑ **Encryption** of data: transforms plaintext data into ciphertext in order to conceal its' meaning
  - ❑ **Signing** of data: computes a *check value* or *digital signature* to a given plain- or ciphertext, that can be verified by some or all entities being able to access the signed data
- ❑ Some cryptographic algorithms can be used for both purposes, some are only secure and / or efficient for one of them.
- ❑ Principal categories of cryptographic algorithms:
  - ❑ **Symmetric cryptography** using 1 key for en-/decryption or signing/checking
  - ❑ **Asymmetric cryptography** using 2 different keys for en-/decryption or signing/checking
  - ❑ **Cryptographic hash functions** using 0 keys (the “key” is not a separate input but “appended” to or “mixed” with the data).

# Attacking Cryptography: Cryptanalysis

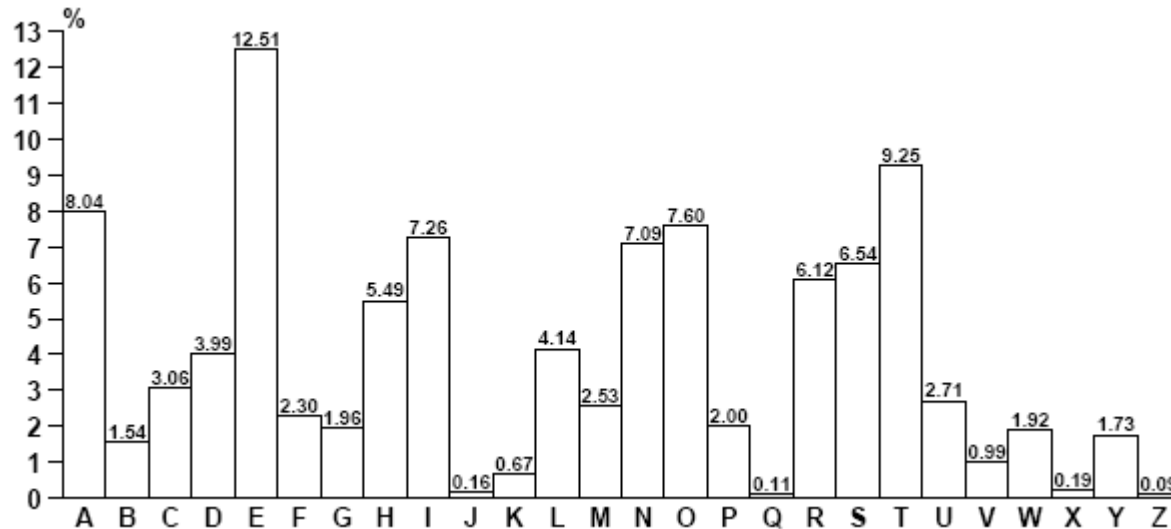


- ❑ *Cryptanalysis* is the process of attempting to discover the plaintext and / or the key
- ❑ Types of cryptanalysis:
  - ❑ *Ciphertext only*: specific patterns of the plaintext may remain in the ciphertext (frequencies of letters, digraphs, etc.)
  - ❑ *Known ciphertext / plaintext pairs*
  - ❑ *Chosen plaintext or chosen ciphertext*
  - ❑ Newer developments: *differential cryptanalysis, linear cryptanalysis*
- ❑ Cryptanalysis of public key cryptography:
  - ❑ The fact that one key is publicly exposed may be exploited
  - ❑ Public key cryptanalysis is more aimed at breaking the cryptosystem itself and is closer to pure mathematical research than to classical cryptanalysis
  - ❑ Important directions:
    - Computation of discrete logarithms
    - Factorization of large integers

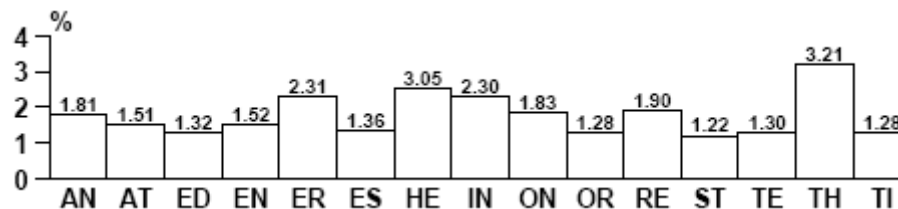
# Attacking Cryptography: Cryptanalysis



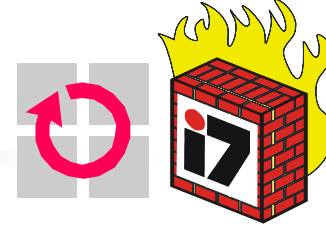
- Frequency of single characters in English text



- Frequency of 15 common digrams in English text (27% overall)



# Attacking Cryptography: Brute Force Attack

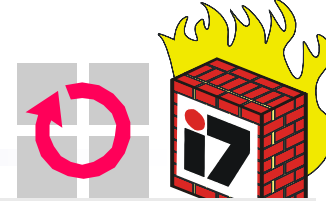


- ❑ The *brute force attack* tries every possible key until it finds an intelligible plaintext:
  - ❑ Every cryptographic algorithm can in theory be attacked by brute force
  - ❑ On average, half of all possible keys will have to be tried

## Average Time Required for Exhaustive Key Search

Key Size [bit]	Number of keys	Time required at 1 encryption / $\mu\text{s}$	Time required at $10^6$ encryption / $\mu\text{s}$
32	$2^{32} = 4.3 * 10^9$	$2^{31} \mu\text{s} = 35.8$ minutes	2.15 milliseconds
56	$2^{56} = 7.2 * 10^{16}$	$2^{55} \mu\text{s} = 1142$ years	10.01 hours
128	$2^{128} = 3.4 * 10^{38}$	$2^{127} \mu\text{s} = 5.4 * 10^{24}$ years	$5.4 * 10^{18}$ years

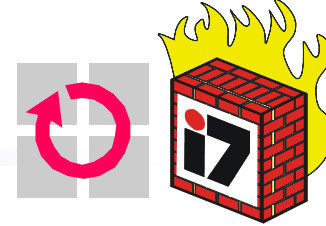
# Attacking Cryptography: How large is large?



## Reference Numbers Comparing Relative Magnitudes

Reference	Magnitude
Seconds in a year	$\approx 3 * 10^7$
Seconds since creation of solar system	$\approx 2 * 10^{17}$
Clock cycles per year (1 GHz computer)	$\approx 3.2 * 10^{16}$
Binary strings of length 64	$2^{64} \approx 1.8 * 10^{19}$
Binary strings of length 128	$2^{128} \approx 3.4 * 10^{38}$
Binary strings of length 256	$2^{256} \approx 1.2 * 10^{77}$
Number of 75-digit prime numbers	$\approx 5.2 * 10^{72}$
Electrons in the universe	$\approx 8.37 * 10^{77}$

# Important Properties of Encryption Algorithms

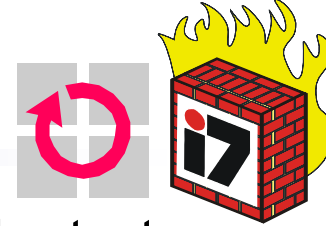


- ❑ Consider, a sender is encrypting plaintext messages  $P_1, P_2, \dots$  to ciphertext messages  $C_1, C_2, \dots$

Then the following properties of the encryption algorithm are of special interest:

- ❑ *Error propagation* characterizes the effects of bit-errors during transmission of ciphertext to reconstructed plaintext  $P_1', P_2', \dots$ 
  - ❑ Depending on the encryption algorithm there may be one or more erroneous bits in the reconstructed plaintext per erroneous ciphertext bit
- ❑ *Synchronization* characterizes the effects of lost ciphertext data units to the reconstructed plaintext
  - ❑ Some encryption algorithms can not recover from lost ciphertext and need therefore explicit re-synchronization in case of lost messages
  - ❑ Other algorithms do automatically re-synchronize after 0 to  $n$  ( $n$  depending on the algorithm) ciphertext bits

# Classification of Encryption Algorithms

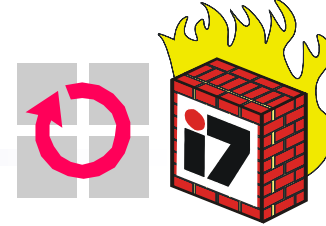


- ❑ The type of operations used for transforming plaintext to ciphertext:
  - ❑ **Substitution**, which maps each element in the plaintext (bit, letter, group of bits or letters) into another element
  - ❑ **Transposition**, which re-arranges elements in the plaintext
- ❑ The number of keys used:
  - ❑ **Symmetric ciphers**, which use the same key for en- / decryption
  - ❑ **Asymmetric ciphers**, which use different keys for en- / decryption
- ❑ The way in which the plaintext is processed:
  - ❑ **Stream ciphers** work on bit streams and encrypt one bit after another:
    - Many stream ciphers are based on the idea of linear feedback shift registers, and there have been detected vulnerabilities of a lot of algorithms of this class, as there exists a profound mathematical theory on this subject.
    - Most stream ciphers do not propagate errors but are sensible to loss of synchronization.
  - ❑ **Block ciphers** work on blocks of width  $b$  with  $b$  depending on the specific algorithm.



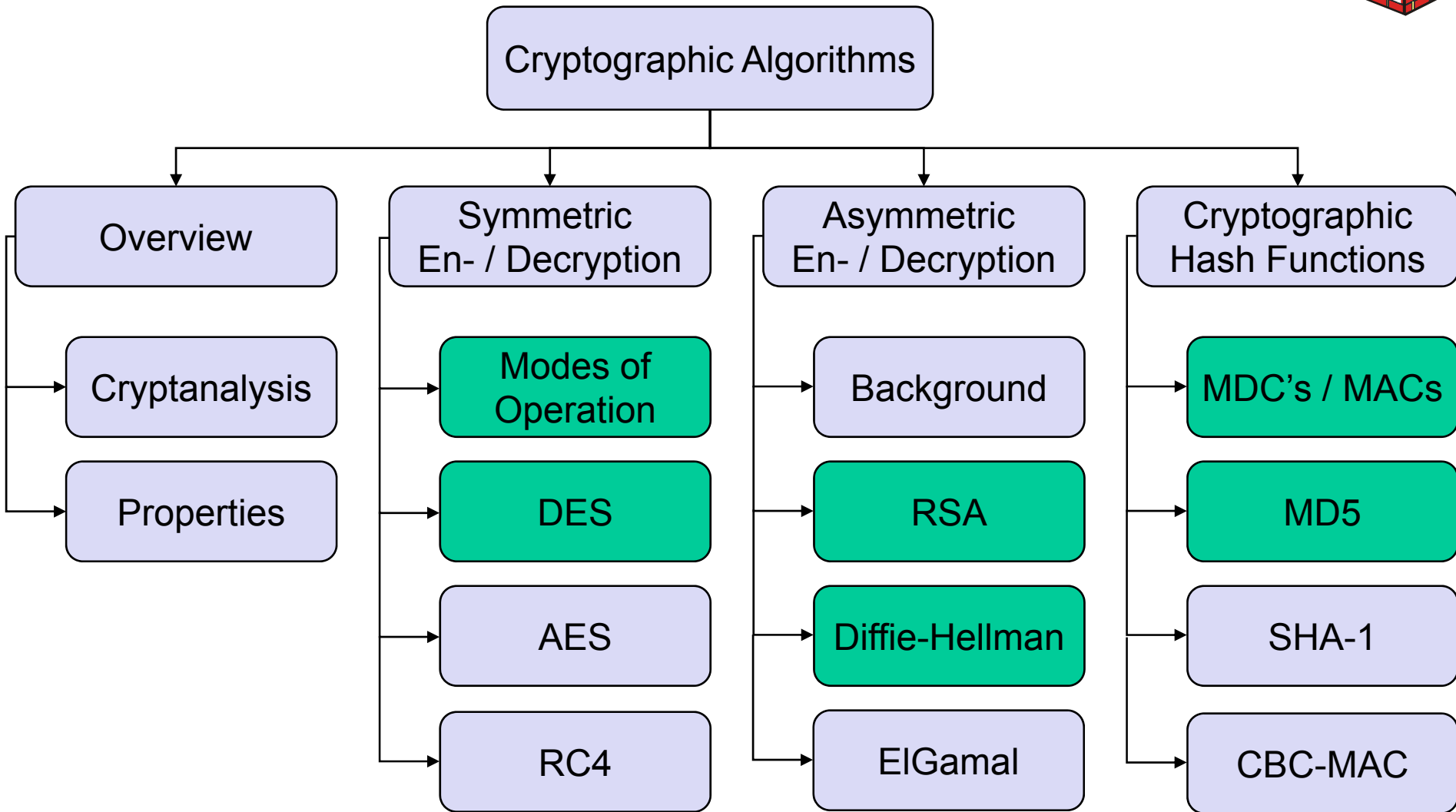
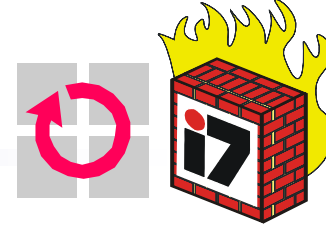
# Key Management

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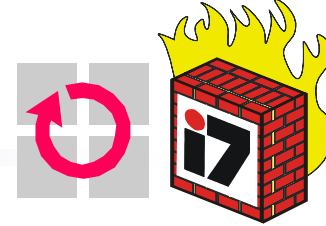
- ❑ Key generation
  - ❑ Must use (pseudo) random number generators
  - ❑ Key generation for asymmetric encryption depends on the factorization of large integer numbers
- ❑ Key distribution
  - ❑ Simplest case: personal contact
  - ❑ Encrypted channel for key distribution -> Key hierarchies
- ❑ Key storage
  - ❑ Optimum case: in the brain of the user
  - ❑ Alternatively, in secured crypto modules
- ❑ Key recovery
  - ❑ Simple case: using a saved copy (implicates new security issues)
  - ❑ Alternatively, fragment the key into several sub-keys
- ❑ Key invalidation
  - ❑ Especially required for asymmetric mechanisms
- ❑ Key deletion
  - ❑ Disablement of old encrypted texts

# Cryptographic Algorithms – Outline



# Summary (what do I need to know)

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- ❑ Categories of cryptographic algorithms
  - ❑ Symmetric encryption
  - ❑ Asymmetric encryption
  - ❑ Cryptographic hash functions
  
- ❑ Application of encryption techniques
  - ❑ Encryption
  - ❑ Signing
  
- ❑ Classification of encryption algorithms
  - ❑ Symmetric vs. asymmetric
  - ❑ Stream vs. block ciphers