

# Concurrent Systems

*Nebenläufige Systeme*

## II. Concurrency

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# Agenda

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Interdependencies

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Summary



## Preface

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- Interdependencies

- Dimensions

## Resource Sharing

- Principles

- Competition

- Synchronisation

## Summary



- discussion on two fundamental **abstract concepts**:
  - concurrency** (Ger. *Nebenläufigkeit*),
    - designates the relation of causal independent events
    - is related to events that have no mutual influence
  - causality** (Ger. *Kausalität, Ursächlichkeit*)
    - designates the relation between cause and effect
    - is the causal chain or connection of two events

## Definition (concurrent)

Events occur or are concurrent if none is the cause of the other.

- explanation of the relation of these concepts to **resource sharing**
  - differentiated with respect to various types of resources and sharing
  - classified as to appropriate or necessary synchronisation paradigms



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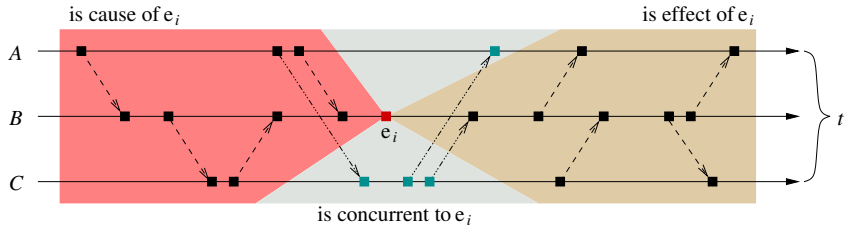
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# Principle of Causality

- causal chain of events related to some other event  $e_i$ :



- $A$ ,  $B$  and  $C$  denote some computation on a private or shared processor
- an event is concurrent to another event ( $e_i$ ) if it lies in the elsewhere of the other event ( $e_i$ )
- the event is neither cause nor effect of the other event ( $e_i$ )
  - as the case may be, it is cause/effect of other events (different from  $e_i$ ) that are lying in the elsewhere (cf. dash-and-dot line)



# Order of Precedence

- computations can be carried out concurrently provided that:
  - general** ■ none requires a result of the other (cf. p. 10)
    - non-existent **data dependencies**
  - special** ■ none depends on delays brought forth by the other
    - deadlines may be missed rarely or under no circumstances
    - periods may be stretched up to a certain limit or not at any time
  - non-existent **timing restrictions**  $\leadsto$  *real-time processing*
- interrelation of computations/events constrains concurrency

## Event correlations v. Processing modes

$\left. \begin{array}{l} \text{"is cause of"} \\ \text{"is effect of"} \end{array} \right\} \mapsto \text{sequential (realised before/at run-time)}$

$\text{"is concurrent to"} \mapsto \text{parallel (realised in logical/real terms)}$

$\hookrightarrow$  decrease of the portion of **sequential code** is an important aspect



# Limits in the Degree of Concurrency

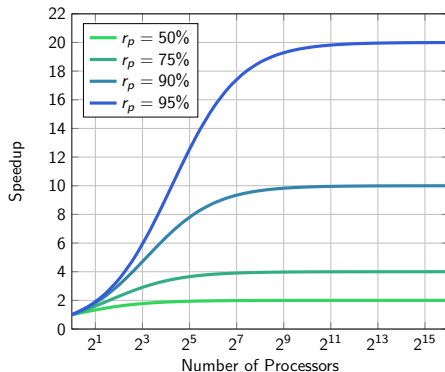
- Amdahl's Law [1]: speed-up ( $su$ ) achievable by parallel processors
  - work load remains constant with the varying number of processors
  - aim at reducing overall computation time for a given fixed-size problem

$$\begin{aligned} su &= (r_s + r_p) / (r_s + \frac{r_p}{n}) \\ &= \frac{1}{r_s + \frac{r_p}{n}} \end{aligned}$$

$r_s$  ratio of sequential code

$r_p$  ratio of parallel code,  
independent of  $n$

$n$  number of processors



- speed-up will be constrained by **data management housekeeping**
  - the nature of this overhead appears to be sequential





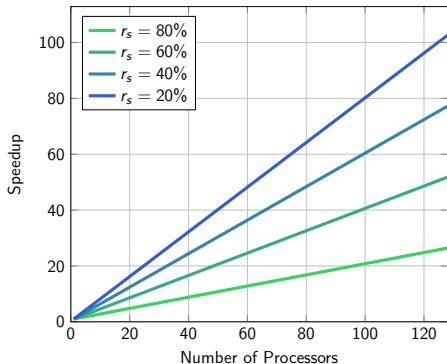
# Adapting the Work Load

- Gustafson's Law [4]: scaled speed-up ( $ssu$ ), "hands-on experience"
  - work load varies linearly with the number of processors
  - aim at getting better results for a given fixed computation time

$$\begin{aligned}ssu &= \frac{r_s + r_p \times n}{r_s + r_p} \\&= r_s + r_p \times n \\&= n + (1 - n) \times r_s\end{aligned}$$

$r_p$  ratio of parallel code,  
scales with  $n$

$r_s, n$  as with Amdahl's Law



- data management housekeeping (serial part) becomes less important
  - in practise, the problem size scales with the number of processors: **HPC**<sup>1</sup>

<sup>1</sup>High Performance Computing



# Concurrent Operations of a Computation

- operations can be concurrent if none needs the result of the other:

```
1  int foo, bar;  
2  
3  int sample(int tupel[2]) {  
4      int subtotal, product;  
5  
6      foo = tupel[0];  
7      bar = tupel[1];  
8  
9      subtotal = foo + bar;  
10     product = bar * foo;  
11  
12     return subtotal + product;  
13 }
```

in computation:

- which statements can be concurrent?
  - 6 and 7
  - 9 and 10
- which statements are not concurrent?
  - (6, 7) and (9, 10)
  - (9, 10) and 12
- defined by the **causal order** (Ger. *Kausalordnung*) of the statements
  - as far as the **logical dimension** of a program is concerned
  - but there is also a **physical dimension**, namely when it comes to the execution of that program by a real processor  $\leadsto$  *level of abstraction*



# Level of Abstraction

- a concurrent operation (in logical terms) at a higher level can be sequential (in real terms) at a lower level
  - the operation handles a resource that can be used only consecutively
    - a single memory area that is shared by multiple computations
    - a single communication bus that is shared by multiple processing units
  - simultaneous executions are constrained by the resource characteristic
- ⇒ may result in a *performance penalty*, non-critical situation **but for...**<sup>2</sup>
- a sequential operation (in logical terms) at a higher level can be “concurrent” (i.e., **non-sequential** in real terms) at a lower level
  - the operation appears to be complex, consists of multiple sub-steps
    - the  $n$ -bit assignment on a  $\frac{n}{2}$ -bit machine, with  $n = 16, 32, 64$
    - the addition of a number to a shared variable located in main memory
  - simultaneous execution of the sub-steps must be considered (cf. p. 18)
- ⇒ reveals a *race condition*, substantial critical situation: **error**

<sup>2</sup>real-time processing, especially in case of hard deadlines.



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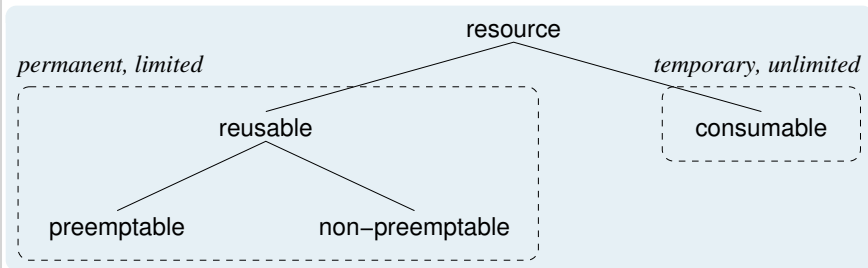
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- permanent<sup>3</sup> resources are **reusable**, but always only of limited supply
  - they are acquired, occupied, used, and released (when no longer required)
    - **in-use resources** are preemptable or non-preemptable, depending on whether allocation to another occupant is possible
  - when non-preemptable, they are exclusively owned by an occupant
- temporary resources are of unlimited supply, they are **consumable**
  - i.e. produced, received, used, and destroyed (when no longer required)

<sup>3</sup>Also referred to as “persistent”.



# Resource Peculiarities

- **hardware resources** as to be managed, e.g., by an operating system

## reusable

- processor ■ CPU, FPU, GPU; MMU
- memory ■ RAM, scratch pad, flash
- peripheral ■ input, output, storage

## consumable

- signal ■ IRQ, NMI, trap

- **software resources** as to be managed by any other program

## reusable

- code ■ critical section/region
- data ■ variable, placeholder

## consumable

- signal ■ notice
- message ■ packet, stream

- reusable data resources are notably **container** for consumable resources
  - the latter must be contained in variables/placeholders to be processible
- availability of the former constrains production/consumption of the latter
- reusable and consumable resources imply different **use patterns**



- if so, **reusable resources** are subject to **multilateral** synchronisation
  - provided that the following two basic conditions (i.e., constraints) apply:
    - i resource accesses by computations may happen (quasi-) simultaneously
    - ii simultaneous accesses may cause a **conflicting state change** of the resource
  - simultaneous use of a **shared resource** this way must be coordinated
    - coordination may affect computations in a blocking or non-blocking manner<sup>4</sup>
- **consumable resources** are subject to **unilateral** synchronisation
  - generally also referred to as logical or conditional synchronisation:
    - logical** – as indicated by the “role playing” of the involved computations
    - conditional** – as indicated by a condition for making computational progress
  - use of a **temporary resource** follows a causal course of events or actions
    - by affecting producers in a non-blocking and consumers in a blocking way
- simultaneous computations **overlap** in time, interfere with each other
  - they become critical in any case if they also overlap in (identical) place

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<sup>4</sup>At the same level of abstraction, use of a shareable resource is exclusive in the blocking case or never refused in the non-blocking case.



- assuming that the following subroutines (put and get) are executed in any order and that they may also run simultaneously:

```
1 char buffer[80];
2 unsigned in = 0, out = 0;
3
4 void put(char item) {
5     buffer[in++ % 80] = item;
6 }
7
8 char get() {
9     return buffer[out++ % 80];
10 }
```

→ in which buffer is a **reusable** and item is a **consumable** resource

- put and get must be subject to uni- and multilateral synchronisation
  - they are not concurrent under the assumption that was made above

- which logical problems exist?
  - buffered items may be overwritten: **overflow**
  - values may be read from an empty buffer: **underflow**
- which other problems exist?
  - **overlapping writes** may go to the same memory location
  - similar to **overlapping reads**, but reverse
  - **overlapping auto-increments** may manifest wrong values





# Serialisation of Simultaneous Computations

- simultaneous computations or operations, resp., are in competition:
  - **sharing** of the same reusable resource(s)
  - **handover** of the same consumable resource(s)

→ in either case hardware and, if applicable, software resources, too
- both aspects, in turn, apply against the background of the following:
  - i the moment of an **simultaneous operation** is not predetermined
  - ii the operation in question is complex (i.e., consists of multiple steps)
  - iii the characteristic of this operation is its **divisibility** in temporal respect
- **conflict-prone operations** must go on *seriatim* (Ger. *nacheinander*)
  - off-line**
    - static scheduling based on control-flow and data dependencies
    - **analytical approach** that takes *a priori* knowledge as given (v.s. i)
    - at run-time, dependable operations are implicitly synchronised
  - on-line**
    - suitable explicit synchronisation of all dependable operations
    - **constructive approach** in shape of a **non-sequential program**
    - based on either pessimistic or optimistic run-time assumptions
- the chosen synchronisation method should be *minimally invasive*



# Divisibility in Temporal Respect

- when the steps of a complex operation may overlap at run-time
  - due to **simultaneous operation** (Ger. *Simultanbetrieb*)
- by way of example an auto-increment operator (cf. p. 16):
  - as compiled from C to ASM (x86): `gcc -O3 -m32 -static -S`

`in++`

`out++`

```
1  movl  _in, %ecx
2  leal  1(%ecx), %eax
3  movl  %eax, _in
```

```
4  movl  _out, %ecx
5  leal  1(%ecx), %eax
6  movl  %eax, _out
```

- non-critical** ■ overlapping execution of `in++` and `out++`  
■ simultaneous operations work on different variables<sup>5</sup>
- critical** ■ self-overlapping execution of `in++` or `out++`, resp.  
■ simultaneous operations work on the same variable<sup>5</sup>
- the critical case may result in **wrong reading** (Ger. *Zählerwert*) of `in/out`
    - `in++` or `out++` are not concurrent to oneself, resp.: they are **not re-entrant**

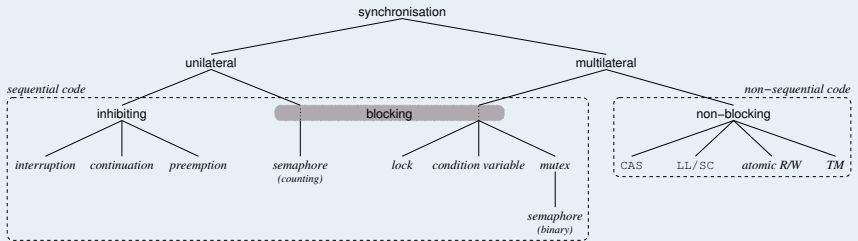
<sup>5</sup> Assuming that processor registers are private to each computation.



- assure a conflict-prone complex operation of (logical) **indivisibility**
  - interpret the equivalent computation as **elementary operation** (ELOP)
    - an operation of indivisible cycle (Ger. *zeitlicher Ablauf*), apparently **atomic**
- indivisibility of a *cycle* is achieved through **synchronisation**,<sup>6</sup> i.e.:
  - i **coordination** of the cooperation and competition between processes X
  - ii **calibration** of real-time clocks or data in distributed systems
  - iii **sequencing** of events along the causal order
- two fundamental approaches to synchronisation are distinguished:
  - blocking** ■ ensure synchronism at **operation start**
    - lock potential overlapping out in the first place
    - synchronised operation is made of sequential code
  - non-blocking** ■ ensure synchronism at **operation end**
    - allow potential overlapping, achieve consistency afterwards
    - synchronised operation is made of non-sequential code
- both approaches come in a variety of solutions to the same problem

<sup>6</sup>(Gr. *sýn*: synced, *chrónos*: time)





- the methods are more or less disruptive of the problematic operation:
  - sequential** ■ bracket sequential code by a **locking protocol** ☹️
    - for the most part, the original code can be reused 😊
    - ➡ *pessimistic*, overlapping is not a rare event
  - non-sequential** ■ reprogram sequential code as a **transaction** 😊
    - for the most part, the original code cannot be reused ☹️
    - ➡ *optimistic*, overlapping is a rare event
- wherever applicable, **downsizing sequential code** is basic
  - i.a. Amdahl's Law (cf. p.8) argues for non-blocking synchronisation



# Synchronisation Behaviour

- effect of synchronisation procedures on the computations involved:
  - inhibiting** ■ prevents other computations from launching
    - irrespective of the eventuality of co-occurrence
    - applies to consumable resources (i.e., signals), only
  - blocking** ■ running computations are not delayed
    - delays computations subject to resource availability
      - takes effect only in case of co-occurrence (overlapping)
      - applies to reusable and consumable resources
    - running computations are possibly delayed
  - non-blocking** ■ may force non-dominantly running computations to repeat
    - takes effect only in case of co-occurrence (overlapping)
    - applies to reusable resources, only
    - dominantly running computations are not delayed
- it bears repeating: ***downsizing sequential code*** is basic
  - where possible, non-blocking synchronisation should be the first choice
- but even then: there is no all-in-one approach for every purpose. . .



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- understanding (Ger.) **Gleichzeitigkeit** in its various meanings:
  - concurrency
    - happening together in time and place [7]
    - designates the relation of causal independent events
    - when none computation depends on results of the other
  - simultaneity
    - occurring, done, existing together or at the same time [7]
    - effect of a certain operation mode of a computing machine
    - causes possibly critical overlapping of computations
  - synchronism
    - fact of being synchronous; simultaneous occurrence [7]
    - in respect of the multiple sub-steps of a complex operation
    - achieved through “ELOOP-ifying” coherent instructions
- simultaneity includes concurrency, but not the other way round
  - concurrency implies unconstrained overlapping in time and place
  - but simultaneity may also cause overlapping that must be constrained
- synchronism ensures that overlapped complex operations do right
  - the individual sub-steps will be strictly executed *interim* (consecutively) or
  - a *transaction* will take care for consistent (pseudo-) parallel execution



- the concept of (distant) simultaneity is not absolute, but depends on the **frame of reference** (Ger. *Bezugssystem*) an observer takes
  - moving- and fixed-platform thought experiment [2, p. 768]:

*The simultaneity of two distant events means a different thing to two different observers if they are moving with respect to each other.*

- the reference frame when reflecting on simultaneous computations is the **level of abstraction** (cf. p. 11) of a particular program section
  - a simplistic operation (++) at a higher level may translate to a complex operation (*read-modify-write*) at a lower level
    - while multiple invocations of the former will take place sequentially,<sup>7</sup> the corresponding ones of the latter may come about non-sequentially
    - while multiple invocations of the latter discretely can be concurrent, their logical correlation to the former makes them possibly not concurrent
  - operations must be resolved **cross-level** (from “fixed platform” observed) in order to realise their ability for concurrency or need for synchronism

<sup>7</sup>Due to the fact that each one refers to an ELOP (cf. p. 19), logically.





- computations can be **concurrent** if none needs a result of the other
  - they must be free of data and control-flow dependencies
- in order to be concurrent, computations must be **simultaneous**
  - quasi-simultaneous through partial virtualisation (hardware multiplexing) or real simultaneous by multiprocessing (hardware multiplication)
  - both techniques will induce computations to overlap in time and place
- **overlapping** in time cause interference but is the lesser of two evils
  - more critical is overlapping **in place** relating to the same resource
  - particularly with regard to the same (i.e., shared) memory area
- critical overlapping must be counteracted through **synchronisation**
  - i.e., coordination of the cooperation and competition between processes
  - here: uni- or multilateral synchronisation, depending on the resource type
- synchronisation ensures for **indivisibility** of a computation cycle
  - at the outset: physical, in blocking manner, by being pessimistic ☹️
  - at the road's end: logical, in non-blocking manner, by being optimistic 😊



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- **bounded buffer** using a counting semaphore [3] for unilateral and an ELOP (x86) for multilateral synchronisation

```
1 typedef int semaphore_t;
2
3 extern void P(semaphore_t*);
4 extern void V(semaphore_t*);
5
6 semaphore_t free = 80;
7 semaphore_t empty = 0;
8
9 static inline int fai(int *ref) {
10     int aux = 1;
11
12     asm volatile("lock; xaddl %0,%1"
13         : "=r" (aux), "=m" (*ref)
14         : "0" (aux), "m" (*ref));
15
16     return aux;
17 }
18
19 char buffer[80];
20 unsigned in = 0, out = 0;
21
22 void put(char item) {
23     P(&free);
24     buffer[fai(&in) % 80] = item;
25     V(&empty);
26 }
27
28 char get() {
29     char item;
30
31     P(&empty);
32     item = buffer[fai(&out) % 80];
33     V(&free);
34
35     return item;
36 }
```

**free** ■ controls the number of unused buffer entries

■ *P* prevents from buffer overflow, *V* signals reusable resource

**empty** ■ controls the number of used buffer entries

■ *P* prevents from buffer underflow, *V* signals consumable resource

**fai** ■ indivisibly *fetch and increment* specified counter variable

